Systems Biology Approach for Mapping TNFα-NFκB Mathematical Model to a Protein Interaction Map

Mahesh Visvanathan^{*,1}, Christian Baumgartner², Bernhard Tilg² and Gerald Henry Lushington¹

¹Bioinformatics Core Facility, University of Kansas, Lawrence, KS 66047, USA ²University for Health Sciences, Medical Informatics and Technology (UMIT) Hall in Tyrol, Austria

> **Abstract:** We investigated different mathematical models concerning signaling pathways and built a new pathway model for TNF α -NF κ B signaling using an integrative analytical approach. This integrative approach consists of a knowledgebase, model designing/visualization and simulation environments. In particular, our new TNF α -NF κ B signaling pathway model was developed based on literature studies and the use of ordinary differential equations and a detailed protein-protein interaction connectivity map within this approach. Using the most detailed mathematical model as a base model, three new proteins -- TRAF1, FLIP, and MEKK3 -- were identified and included in our new model. Our results show that this integrative approach offers the most detailed and consistent mathematical description for TNF α -NF κ B signaling and further increases the understanding of TNF α -NF κ B signaling pathway. This tool can be downloaded through the following link (http://sourceforge.net/projects/dmsp11/).

Keywords: TNF α mediated NF- κ B signaling pathway, protein-protein interaction and mathematical model.

INTRODUCTION

Interactions of molecules are essential for almost all cellular functions. Genes and proteins seldom carry out their functions in isolation. They operate through a number of interactions with other biomolecules. Molecular interactions in biological pathways and networks are highly dynamic and may be controlled by feedback loops and forward regulation mechanisms as well as interlinks with other cellular hierarchies. They make experimental elucidation and computational analysis of pathways extremely challenging. Mathematical modeling is becoming increasingly important as a tool to capture molecular interactions and dynamics from high-throughput experiments. Biological pathways and networks are often represented graphically. Ordinary differential equations (ODEs) have been commonly used to help explain the kinetic process of association and disassociation among molecules in chemical or biochemical reactions.

Tumor necrosis factor-alpha (TNF α) is a cytokine involved in systematic inflammation and is a member of a group of cytokines that all stimulate the acute phase reaction. Dysregulation and over-production of TNF α have been implicated in the pathogenesis of a wide spectrum of human diseases, e.g. sepsis, diabetes, cancer, osteoporosis, multiple sclerosis and crohns disease. Eliminating TNF α by a specific monoclonal antibody, e.g. infliximab, caused dramatic effects on the phenotype of the diseases, with severe side effects. To find specific ways with least side effects to block or partially block TNF α actions, we need to learn more about the signaling pathways of TNF α . Some research efforts have been shifted from intercellular to intracellular signaling in order to increase the knowledge about the involved cell proteins and to get a better understanding of the molecular dynamics of the TNF α -related pathways, especially the TNF α -NF κ B signaling pathway.

Biological cartoons and analytical pathway models have been constructed for the TNFa-NFkB signaling pathway respectively. These models can be used for computer simulation studies in order to get insights on setting various experimental scenarios. The better understanding of diseases makes the drug development more appropriate with minimal side effects [1, 2]. Reliable information about proteins and molecular interactions of the signaling pathway is needed to improve the structure of a pathway model. It has known that several protein purification methods are not capable of detecting protein activities in natural concentration. Because of protein over-expression, non-natural protein complex building can occur [3, 4] which could cause faults in modeling. Although a significant amount of biological and biochemical literature is now available in this research field, some of which examine only small parts of the pathway and sometimes with methods relying on over-expression situations. In this paper, we introduce an integrative approach to analyze experimental TNFa-NFkB signaling pathway model. We built an integrative database that includes mathematical modeling data, literature information as well as biological data. In particular, the modeling data consists of kinetic constants, kinetic equations and initial concentrations for building mathematical ODE models. The biological data includes descriptions of proteins, proteinprotein interactions and other information concerning signaling pathways. All information can be retrieved and visualized within our integrative computational framework. The paper is organized as follows: Section 2 provides our methodology and delimitates the modeling of the TNFa-NFkB signaling pathway based on ODE models and the literature information. Section 3 describes the results

^{*}Address correspondence to this author at the Bioinformatics Core Facility, University of Kansas, Lawrence, KS 66047, USA; Tel: 785-864-3337; Fax: 785-864-8141; E-mail: mvisvanathan@ku.edu

obtained from our extended TNF α -NF κ B signaling pathway model. Section 4 gives our discussion and conclusion of this work.

MATERIALS AND Methodology

Integrating Heterogeneous Information for Modeling

The immunosuppression associated with neutralization of TNF α through infliximab results in serious adverse effects e.g. systemic tuberculosis, allergic granulomatosis of the lung, or mild leucopenia in patients with active ankylosing spondylitis [5]. Because of these clinical adverse effects, additional information on the mechanisms of the action of infliximab is needed. In order to increase understanding of the mechanism of TNF α , to find more specific drug targets, to minimize adverse effects and to maintain the duration of the treatment, the focus of attention in research has been shifting from intercellular signals such as TNF α , to intracellular signals, such as the signal transduction pathway from the membrane receptors of TNF α to the transcription factors AP1 and NF κ B and to apoptosis.

The exact description of the TNF α pathway is no easy task. Various publications on this topic exist, but they lack focus on the interactions of all the proteins in the pathway. Evidence for the uncertainty about the pathway structure is provided by lots of different biological cartoons dealing with TNF α and NF κ B [6-16]. Some of these cartoons use quite different proteins. A recently developed method, the TAP (tandem affinity purification) tag strategy [17, 18], seems to overcome some of the problems and opens a new door in large scale experiments. Further problems have been due to the fact that a lot of experiments were based on protein over-expression situations, which can produce non-physiological complex building. This problem is also solved by the TAP tag strategy [6].

The development of a precise mathematical model is a very difficult task. As the biological knowledge and the experimental data used are insufficient, various assumptions have to be made concerning kinetic parameters and concentrations of proteins involved. The first step to produce a mathematical model is to develop a detailed qualitative model or a cartoon outlining participating proteins after collecting biological and experimental data. This qualitative model/cartoon has to be translated into a quantitative mathematical model [19]. There are two principle ways to construct mathematical models to model the kinetics of biochemical reactions: a deterministic formulation based on nonlinear ordinary differential equations (ODEs) for large numbers of molecules and a stochastic formulation rooted in exponential distribution law. Deterministic models have been commonly used as they can be easily applied with existing off-the-shelf computer software programs, while stochastic models are currently getting more attention and being further developed to capture certain randomness nature of molecular interactions [20, 21]. The alternative to stochastic simulation is using Gillespie's algorithm, which is an event-driven simulation where the time of next event is exponentially distributed is also used.

A pathway cartoon comprises only qualitative information of the biochemical pathway of interest (e.g. the TNF α -NF κ B signaling pathway in our work). The proteins

in the cartoon are placed in the region where they are situated in the cell, e.g. the receptor is at the cell membrane, the interacting proteins, which may be located in the cell nucleus, are far away. Information about protein interactions and complex building is hidden in the biological cartoons. Such cartoons do not explain molecular dynamics quantitatively, but they provide a schematic visual overview of the overall dynamics and information processing in cellular systems. Mathematical models of a biochemical pathway can show the chronology of protein complex association and dissociation. This is done with respect to the initial concentrations of the proteins and the kinetic parameters that control the simulation and analysis of theses models [22-26]. Protein-protein interaction connectivity maps also provide important information on which proteins are co-purified with distinct target proteins. To compare and integrate the pathway mathematical model with the proteinprotein interaction connectivity maps is a challenge. Based on various cartoons of the TNF α -NF κ B signaling pathway, we identified the graphical dynamics of protein complex building. A graphic presentation of a qualitative pathway model of the TNF α -NF κ B signaling pathway is shown in Fig. (1).

Architecture of the Integrative Framework

Our integrative framework was designed as a 3-tier architecture shown in Fig. (2). It consists of a Java-based designing-visualization environment and pathway а simulation environment in the upper application tier, a Java Database Connectivity-Open Database Connectivity (JDBC-ODBC) in the middle tier, and a relational data management system in the back-end database tier. Within this framework we first designed the TNF α -NF κ B pathway model in the designing-visualization environment that allows inclusion of mathematical modeling data, simulation data and biological data from our integrated knowledgebase in the database tier. Then, the designed $TNF\alpha$ -NF κ B pathway model was exported in an XML format from the designing environment to the simulation environment.

The organizational structure of the database tier was designed to represent different levels of data. The entities of the knowledgebase contain information grouped into three categories: molecular components, reactions and pathways. These entities inherit both, the biological and modeling information concerning specified pathways. Specifically, the knowledgebase incorporates biological knowledge about components, reactions and pathways from three different online external protein databases: Biomolecular Interaction Network Database (BIND) [27, 28] Database of Interacting Proteins (DIP) [29] and Munich Information Center for Protein Sequences (MIPS) protein-protein interaction database [30] as well as internal experimental verifications and literature studies.

The mathematical modeling knowledge includes kinetic constants, kinetic equations and initial concentrations and is related to the components and reactions of the pathway under investigation (e.g. $TNF\alpha$ -NF κ B signaling pathway in our work). In general deterministic formulation, mathematical models of pathways use differential equations relying on fundamental assumptions. For example, a signal transduction system behaves as a slowly time varying non-



Fig. (1). The TNF α pathway model that was developed by our framework, it incorporates biological and modelling knowledge.

linear system during a reaction period based on biological observations. Further, it is assumed that a cell keeps the concentration of each signaling protein constant before and after each signaling, that is the concentration of these proteins return to steady state after the reaction. With these assumptions on molecular kinetics, the ordinary differential equations for the mathematical models are derived and stored for simulation of the signaling pathway of interest. We have derived a new ODE model by also incorporating protein-protein interaction connectivity map information for the TNF α -NF κ B signaling pathway with our integrative analysis. Simulations and analyses were done using a graphical user interface that was designed and developed using *MATLAB*[®]. More details explained in the results section.

RESULTS

For signaling pathway modeling, the following problems occur:

- It is not clear, which proteins should be used to set up a stable model basis, which can easily be extended?
- How is the chronology of protein interactions and which proteins build up a complex?
- How fast and long do the proteins interact (this means, what are the kinetic parameters)?

These problems play a major role in modeling the TNF α -NFkB signaling pathway within our framework. The mathematical models described in [23, 25, 31] related to TNF α pathway showed us that these models contain similar proteins and the general dynamics of complex building was almost identical. Among these models we identified the model based on Cho (we referred it as Model A) as the best available model for possible further improvement in order to address pathway modeling problems mentioned previously. Several other possible extensions/improvements for the pathway Model A were also identified depending on research foci and we concluded that three new proteins -TRAF1, FLIP, and MEKK3 - should be included for possible improvement of Model A. The main focus of our work was to model the TNF α - NF κ B signaling pathway starting from TNFα receptor to the transcription factor AP1, rather than going into other levels. By including the three new proteins, we derived an initial extended pathway model using our integrated analytical framework as shown in Fig. (3).

It is worth mentioning that TRAF1 and FLIP were also considered in the mathematical models by Schöberl, Ihekwaba and MEKK3 has been intensively discussed [25, 31]. All proteins contained in the cell proliferation module of the extended pathway model were identified and compared among others *via* the TAP tagged strategy and the protein-



Fig. (2). The framework was designed in the form of a 3-tier architecture system that includes a Java-based pathway designing, simulation and visualization environments as the upper application tier, JDBC-ODBC middle tier, and an integrative database as the backend tier.

protein interaction connectivity map [32]. We noted that some basic interactions, which were modeled, could not be found in the protein-protein interaction connectivity map (i.e. TNFR1-TRADD, TRADD-FADD, TRADD-RIP, RIP-Caspase8 and RIP-IKK). Since cIAP has not been further examined, the interaction with effector Caspases was not modeled. We resulted with a final ODE pathway model (we referred this final ODE pathway model, Model B).

In Model B, several single proteins like TNFR1, TRADD, RIP1, TRAF2, IKK, IkB and NFkB were identified in the protein-protein interaction connectivity map (Fig. 4). The connectivity map comprises no complexes, only individual proteins. IKK is presented by its subunits $IKK\alpha$, IKK β and IKK γ , colored lilac, and I κ B is presented by its subunits IkBa, IkBβ and IkBε, colored orange. NFkB's family members (monomers) are colored red and their precursors are mentioned in the connectivity map, i.e. NFkB1 (p50; precursor: p105), NFkB2 (p52; precursor: p100), p65 (RelA), c-Rel (Rel), and RelB. All these seven proteins in both the Model B and the connectivity map. With limited experimental data, further modeling improvements are very difficult. The incorporated biological and modeling knowledge are retrieved from the knowledgebase and integrated into the extended TNF α -NF κ B signaling pathway model within our framework.

We performed a systematic examination of the TNF α -NF κ B signaling pathway by simulating different scenarios to

analyze the sensitivity of the Model B with respect to possible changes of the kinetic parameters. The extended TNFα-NFκB signaling pathway model B now including all three new components namely the proteins: MEKK3, FLIP and TRAF1 is indeed quite a stable model. TRAF1 and Caspase8* are reversible from the complex proteins and TRAF1 is irreversibly cleaved and TRAF1c and Caspase8* were yielded. The comparison of the protein concentrations was also performed by plotting the concentrations of the components of other existing mathematical models including model by Cho [24], i.e. Model A, models by Schöberl [31] and Ihekwaba [25] and the new Model B side-by-side. Components, which show extraordinary differences, were examined via further literature investigations. As a result, our extended TNF α -NF κ B signaling pathway model B appears to be the most detailed and consistent mathematical model with protein-protein interaction connectivity information incorporated in it.

DISCUSSIONS

Complex interactions of intracellular proteins regarding time course and protein concentrations as well as kinetic behaviors cause high variability in biological functions. To bring light to these complex interaction systems inside of cells, we first have to identify the involved proteins and then to model their interactions by means of sufficient techniques. TNF α is a cytokine, which is implicated in the pathogenesis of various human diseases and therefore it has been under



Fig. (3). The new TNF α -NF κ B pathway model (Model B) includes three new proteins MEKK3 (m32), FLIP (m33) and TRAF1 (m35). Circles (with m and a number) represent various states for protein concentration (i.e. kinetic constants), and directed arrows represent dynamic relations (i.e. kinetic equations). The protein complex TNF/TNFR1/TRADD/RIP1/TRAF2/MEKK3/IKK connects to NF κ B is colored red. The new protein complexes are colored magenta, e.g. Caspase8/FLIP (m34), RAF1/Caspase8* (m36) and TRAF2/TRAF1c (m38).

intense investigations for better understanding of the exact signal flow.

Objective of this work was to build a new TNF α - NF κ B signaling pathway model that allows integration of proteinprotein interaction connectivity map. The mathematical models relating to the TNF α -NF κ B signaling pathway contained similar proteins and identical concept behind complex building. Bouwmeester *et al.* [32] published a connectivity map giving a detailed view on protein-protein interactions of the TNF α -NF κ B signaling pathway on a physiological protein concentration level and this map was used, compared and studied with our extended mathematical model.

Mathematical models based on Cho [24], Schöberl [31] and Ihekwaba [25] are available in relation to $TNF\alpha$ - $NF\kappa B$ signaling pathway. Improvements of the existing pathway models are very difficult and challenging. The decision to use the mathematical model by Cho (i.e. Model A) as our base model and extending it was based on the facts that it is the most detailed mathematical model available today for TNF α - NF κB signaling starting from TNF α receptor up to the transcription factor AP1. The Schöberl [24] and



Fig. (4). The protein-protein interaction connectivity map (Bouwmeester *et al.* 2004). The proteins that are colored are modeled in our new $TNF\alpha$ -NF κ B signaling pathway model B.

Ihekwaba [14] models describe signaling from IKK and NF κ B level onwards. The Ihekwaba's model is

concentrating more into the details of modeling IKK interactions rather than the $TNF\alpha$ -NF κ B signaling.

Mapping TNF &-NF KB Mathematical Model to a Protein Interaction Map

Having selected Model A for extension, we found out that this model contained several inconsistencies, regarding the "recycling" of particular proteins after protein complex dissociation for TNF α - NF κ B signaling pathway as a whole. Model A did not provide valid reasons why they constructed their model in a particular way. We identified some inconsistencies and corrected the model accordingly with information from the protein-protein interaction connectivity map. In the extended Model B these, inconsistencies were abolished. Hence, this extended model can serve as a more consistent mathematical description to reflect TNFa- NFkB signaling pathway. Our overall integrative analytical approach can also be used to more easily compare and study other future models for further modeling improvements as more experimental data become available. In essence, the knowledgebase of our integrative framework will grow accordingly.

Three new proteins – TRAF1, FLIP, and MEKK3 – were included into the extended model B. TRAF1 and FLIP were already considered in the Schöberl model and MEKK3 has also been intensively discussed in the TNF α - NF κ B signaling pathway literature. The importance of this protein has also been pointed out by Bouwmeester *et al.* [32]. The exact localization of MEKK3 in the signaling pathway and the interactions with other proteins are not fully clear at the moment. That is why the actual position in the extended pathway model has to be regarded as a first approximation to nature.

CONCLUSION

One of the main goals of this work was to use the information of the protein-protein interaction connectivity map to build an improved pathway model. In practice, we found that several protein interactions mentioned in literature could not be found in the connectivity map provided by Bouwmeester et al. [32]. Especially, these were the interactions which are situated in close proximity to the cell membrane. On this regard, the connectivity map just outlines which proteins are parts of the TNFa- NFkB signaling pathway, but does not exactly specify all the occurring interactions between them. To construct a valid mathematical model, it is necessary to have a complete view on the interactions in the signaling pathway. If all the important interactions are revealed, this might require changing the general model structure, as the connectivity map suggests several alternative inhibiting and activating signal flow paths, which have not been modeled yet.

The limitation of experimental data also makes it more challenging to develop a pathway model only for TNF α -NF κ B signaling pathway. Information of several sources has to be combined and adapted to fit into one pathway model. Hence, this task makes the possibility of combining models more challenging and interesting. Stochastic mathematical modeling approach is also an interest of our research, and we are currently working on extending a Bayesian probabilistic graphical model framework [21] for TNF α -NF κ B signaling pathway. The validation of the structure of TNF α -NF κ B signaling pathway by means of experimental data and simulation studies are our on-going work in order to get a more physiologically realistic model. This can be done by incorporating experimental data into the knowledgebase and analyzing the pathway models. It is an iterative interplay between experimental analysis and modeling strategies. Simulation results done on signaling pathways will enable us to interpret the biological system from a global systemic view. This will further increase the understanding of signaling pathways.

ACKNOWLEDGEMENT

This project was supported by Award Number P20 RR016475 from the National Center for Research Resources.

REFERENCES

- Kitano H. Computational systems biology. Nature 2002; 420: 206-10.
- You L. Toward computational systems biology. Cell Biochem Biophys 2004; 40: 167-84.
- [3] Rivkin E, Cullinan EB, Tres LL, et al. A protein associated with the manchette during rat spermiogenesis is encoded by a gene of the TBP-1 like subfamily with highly conserved ATPase and protease domains. Mol Reprod Dev 1997; 48: 77-89.
- [4] Swaffield JC, Melcher K, Johnston SA. A highly conserved ATPase protein as a mediator between acidic activation domains and the TATA-binding protein. Nature 1995; 374: 88-91.
- [5] Su CG, Lichtenstein GR. Influence of immunogenicity on the longterm efficacy of infliximab in Crohn's disease. Gastroenterology 2003; 125: 1544-46.
- [6] Bonizzi G, Karin M. The two NF-kappa B activation pathways and their role in innate and adaptive immunity. Trends Immunol 2004; 25: 280- 8.
- [7] Chung JY, Lu M, Yin Q, *et al.* Structural revelations of TRAF2 function in TNF receptor signaling pathway. Adv Exp Med Biol 2007; 597: 93-113.
- [8] Dempsey PW, Doyle SE, He JQ, et al. The signaling adaptors and pathways activated by TNF superfamily. Cytokine Growth Factor Rev 2003; 14: 193-209.
- [9] Dixit V, Mak TW. NF-kappa B signaling. Many roads lead to madrid. Cell 2002; 111: 615-19.
- [10] Micheau O, Tschopp J. Induction of TNF receptor I-mediated apoptosis via two sequential signaling complexes. Cell 2003; 114: 181-90.
- [11] Min JK, Kim YM, Kim SW, et al. TNF-related activation-induced cytokine enhances leukocyte adhesiveness: induction of ICAM-1 and VCAM-1 via TNF receptor-associated factor and protein kinase C-dependent NF-kappaB activation in endothelial cells. J Immunol 2005; 175: 531-40.
- [12] Pomerantz JL, Baltimore D. Two pathways to NF-kappaB. Mol Cell 2002; 10: 693-95.
- [13] Vilimas T, Mascarenhas J, Palomero T, et al. Targeting the NF kappaB signaling pathway in Notch1-induced T-cell leukemia. Nat Med 2007; 13: 70-7.
- [14] Schlosser PM. Experimental design for parameter estimation through sensitivity analysis. J Toxicol Environ Health 1994; 43: 495 -530.
- [15] Wang CY, Mayo MW, Korneluk RG, et al. NF-kappaB antiapoptosis: induction of TRAF1 and TRAF2 and c-IAP1 and c-IAP2 to suppress caspase-8 activation. Science 1998; 281: 1680-83.
- [16] Yao J, Duan L, Fan M, et al. NF-kappaB signaling pathway is involved in growth inhibition, G2/M arrest and apoptosis induced by Trichostatin A in human tongue carcinoma cells. Pharmacol Res 2006; 54: 406-13.
- [17] Cox DM, Du M, Guo X, *et al.* Tandem affinity purification of protein complexes from mammalian cells. Biotechniques 2002; 33: 267.
- [18] Gregan J, Riedel CG, Petronczki M, et al. Tandem affinity purification of functional TAP tagged proteins from human cells. Nat Prot 2007; 2: 1145-51.
- [19] Phair RD. Development of kinetic models in the nonlinear world of molecular cell biology. Metabolism 1997; 46: 1489-95.
- [20] Wolkenhauer O, Cho KH. Analysis and modeling of signal transduction pathways in systems biology. Biochem Soc Trans 2003; 6: 1503-9.
- [21] Wang J, Cheung LW, Delabie J. New probabilistic graphical models for genetic regulatory networks studies. J Biomed Inform 2005; 38: 443-55.

- [22] Barken D, Wang CJ, Kearns J, et al. Comment on oscillations in NF-kappaB signaling control the dynamics of gene expression. Science 2005; 308: 52.
- [23] Cho H, Shin Y, Kolch W, *et al.* Experimental design in systems biology based on parameter sensitivity analysis with monte carlo simulation: a case study for the TNFα mediated NF-κB- signal transduction pathway. Simulation 2003a; 12: 726-39.
- [24] Cho KH, Shin SY, Lee HW, et al. Investigations into the analysis and modeling of the TNF alpha-mediated NF-kappa B signaling pathway. Genome Res 2003b; 13: 2413 -22.
- [25] Ihekwaba AE, Broomhead DS, Grimley RL, et al. Sensitivity analysis of parameters controlling oscillatory signalling in the NFkappa B pathway: the roles of IKK and IkappaBalpha. Syst Biol (Stevenage) 2004; 1: 93-103.
- [26] Nelson DE, Ihekwaba AE, Elliott M, et al. Oscillations in NFkappaB signaling control the dynamics of gene expression. Science 2004; 306: 704-8.

Received: November 3, 2009

Revised: January 1, 2010

Accepted: March 1, 2010

© Visvanathan et al.; Licensee Bentham Open.

This is an open access article licensed under the terms of the Creative Commons Attribution Non-Commercial License (http://creativecommons.org/licenses/by-nc/3.0/) which permits unrestricted, non-commercial use, distribution and reproduction in any medium, provided the work is properly cited.

- [27] Alfarano C, Andrade CE, Anthony K. The biomolecular interaction network database and related tools 2005 update. Nucleic Acids Res 2005; 33: D418-24.
- [28] Gilbert D. Biomolecular interaction network database. Brief Bioinform 2005; 6: 194-8.
- [29] Salwinski L, Miller CS, Smith AJ, Pettit FK, Bowie JU, Eisenberg D. The Database of Interacting Proteins: 2004 update. NAR 32 Database issue: D449-51.
- [30] Pagel P, Kovac S, Oesterheld M, et al. The MIPS mammalian protein-protein interaction database. Bioinformatics 2005; 21: 832-34.
- [31] Schoeberl B, Gilles ED, Scheurich P. A Mathematical vision of TNF receptor interaction. Proceedings of the International Congress of Systems Biology 2001; pp. 158-67.
- [32] Bouwmeester T, Bauch A, Ruffner H, *et al.* A physical and functional map of the human TNF alpha/NF-kappa B signal transduction pathway. Nat Cell Biol 2004; 6: 97-105.